Reg. No. : $\qquad$
Name : $\qquad$

## SECOND YEAR HIGHER SECONDARY EXAMINATION, MARCH 2022

Part - III
MATHEMATICS - SCIENCE Cool-off time : 15 Minutes
Maximum : 60 Scores

## General Instructions to Candidates :

- There is a 'Cool-off time' of 15 minutes in addition to the writing time.
- Use the 'Cool-off time' to get familiar with questions and to plan your answers.
- Read questions carefully before answering.
- Read the instructions carefully.
- Calculations, figures and graphs should be shown in the answer sheet itself.
- Malayalam version of the questions is also provided.
- Give equations wherever necessary.
- Electronic devices except non-programmable calculators are not allowed in the Examination Hall.














## PART - I

## A. Answer any 5 questions from 1 to 9. Each carries 1 score.

1. Which of the following relations on $\mathrm{A}=\{1,2,3\}$ is an equivalence relation?
(a) $\{(1,1),(2,2),(3,3)\}$
(b) $\{(1,1),(2,2),(3,3),(1,2)\}$
(c) $\{(1,1),(3,3),(1,3),(3,1)\}$
(d) None of these
2. The value of $\sin ^{-1}\left(\sin \left(\frac{1}{2}\right)\right)=\ldots$.
(a) $\frac{1}{2}$
(b) $\pi-\frac{1}{2}$
(c) $-\frac{1}{2}$
(d) $\frac{\pi}{6}$
3. If A is a $3 \times 3$ matrix, then $|\operatorname{adj}(\mathrm{A})|=\ldots$
(a) $|\mathrm{A}|$
(b) $|A|^{2}$
(c) $|A|^{3}$
(d) $3|\mathrm{~A}|$
4. $\quad$ A fair die is rolled. If the events are $E=\{1,3,5\}, F=\{2,3\}$, then $P(E \mid F)=\ldots$
5. The area bounded by the curve $\mathrm{y}=2 x$ between $x=0, x=2$ and $x$-axis is ...
6. Slope of the tangent to the curve $\mathrm{y}=x^{2}+1$ at the point $(2,5)$ is ....
7. Write the vector from the point $\mathrm{A}(1,3,5)$ to $\mathrm{B}(4,3,2)$.
8. Which of the following is a point on the plane $3 x+2 \mathrm{y}+4 \mathrm{z}=0$ ?
(a) $(1,2,1)$
(b) $(2,3,2)$
(c) $(2,1,-2)$
(d) $(2,1,2)$
9. Write the degree of the differential equation $2 \frac{d^{2} y}{d x^{2}}+\left(\frac{d y}{d x}\right)^{3}=0$.

## PART - I

## 

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(a) $\{(1,1),(2,2),(3,3)\}$
(b) $\{(1,1),(2,2),(3,3),(1,2)\}$
(c) $\{(1,1),(3,3),(1,3),(3,1)\}$
(d) ஹவயிேேறைอீ
2. $\sin ^{-1}\left(\sin \left(\frac{1}{2}\right)\right)$ ๙ฺஜீ விம $=\ldots$.
(a) $\frac{1}{2}$
(b) $\pi-\frac{1}{2}$
(c) $-\frac{1}{2}$
(d) $\frac{\pi}{6}$

(a) $|\mathrm{A}|$
(b) $|A|^{2}$
(c) $|A|^{3}$
(d) $3|\mathrm{~A}|$




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(a) $(1,2,1)$
(b) $(2,3,2)$
(c) $(2,1,-2)$
(d) $(2,1,2)$

B. Answer all questions from 10 to 13. Each carries 1 score.
10. The value of $\sin ^{-1}\left(\frac{1}{\sqrt{2}}\right)=\ldots$
11. The vertices of a triangle are $(0,2),(0,3),(4,6)$, then area of the triangle is $\qquad$ .
(a) 1
(b) 2
(c) 3
(d) 4
12. Find the direction cosines of the vector $3 \hat{i}-2 \hat{j}+5 \hat{k}$.
13. Derivative of $\log \left(x^{3}\right)$ is ...

## PART - II

A. Answer any 2 questions from 14 to 17. Each carries 2 scores.
14. $\left[\begin{array}{ll}x+y & 2 \\ 5+x & 8\end{array}\right]=\left[\begin{array}{ll}5 & 2 \\ 6 & 8\end{array}\right]$, find $x$ and $y$.
15. The length $x$ of a rectangle is increasing at the rate of $4 \mathrm{~cm} / \mathrm{s}$ and the width y is decreasing at the rate of $5 \mathrm{~cm} / \mathrm{s}$. Find the rates of change of its area when $x=10 \mathrm{~cm}$ and $y=5 \mathrm{~cm}$.
16. Show that the function $\mathrm{f}(x)=x^{3}+3 x+5$ is strictly increasing on R .
17. Solve the differential equation $\frac{\mathrm{dy}}{\mathrm{dx}}=\frac{2 x}{\mathrm{y}^{2}}$.
B. Answer any 2 questions from 18 to 20. Each carries $\mathbf{2}$ scores.
18. Find the value of $\lambda$ if the vectors $\hat{i}-\hat{j}+\hat{k}, 3 \hat{i}+\hat{j}+2 \hat{k}$ and $\hat{i}+\lambda \hat{j}-3 \hat{k}$ are coplanar.
19. If $y=x^{\sin x}$, find $\frac{d y}{d x}$.
20. Find the integrating factor of the differential equation $x \frac{\mathrm{dy}}{\mathrm{d} x}-\mathrm{y}=2 x^{2}$.


$(4 \times 1=4)$
10. $\sin ^{-1}\left(\frac{1}{\sqrt{2}}\right)$ ๑ก్ర8 விఅ $=\ldots$

(a) 1
(b) 2
(c) 3
(d) 4


PART - II






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## PART - III

A. Answer any 3 questions from 21 to 24. Each carries 3 scores.
21. Express the matrix $\mathrm{A}=\left[\begin{array}{ccc}3 & 3 & -1 \\ -2 & -2 & 1 \\ -4 & -5 & 2\end{array}\right]$ as the sum of a symmetric matrix and a skew symmetric matrix.
22. $\mathrm{R}=\{(x, \mathrm{y}): x, \mathrm{y} \in \mathrm{Z},(x-\mathrm{y})$ is an integer $\}$. Show that R is an equivalence relation.
23. Bag 1 contains 5 red and 3 black balls while another Bag 2 contains 3 red and 7 black balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from Bag 2.
24. Consider the vector $\vec{a}=2 \hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=\hat{i}+\hat{j}+\hat{k}$.
(a) Find $\vec{a} \times \vec{b}$
(b) Find a unit vector perpendicular to $\vec{a}$ and $\vec{b}$.
B. Answer any 2 questions from 25 to 27. Each carries $\mathbf{3}$ scores.
25. Using elementary operations, find the inverse of the matrix $A=\left[\begin{array}{ll}1 & 3 \\ 2 & 7\end{array}\right]$.
26. If $*$ is a binary operation on R defined by $\mathrm{a} * \mathrm{~b}=\frac{\mathrm{ab}}{3}$,
(a) Find the identity element of *.
(b) Find the inverse of 3 .
27. Evaluate $\int_{0}^{2} x^{2} \mathrm{~d} x$ as the limit of a sum.

## PART - III

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(3 \times 3=9)
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## PART - IV

## A. Answer any 3 questions from 28 to 31. Each carries 4 scores.

28. Show that $2 \tan ^{-1}\left(\frac{1}{2}\right)+\tan ^{-1}\left(\frac{1}{7}\right)=\tan ^{-1}\left(\frac{31}{17}\right)$.
29. Find the area of the region bounded by $y^{2}=9 x, x=2, x=4$ and the $x$-axis in the first quadrant.
30. (a) Discuss the continuity of the function $\mathrm{f}(x)=\left\{\begin{array}{ll}3 x+1 & \text { if } x \leq 3 \\ x^{2}+1 & \text { if } x>3\end{array}\right.$.
(b) Verify Rolle's theorem for the function $\mathrm{f}(x)=2 x^{2}-12 x+1$ in [2, 4].
31. (a) Find the equation of the line passing through the points $(2,1,0)$ and $(4,4,3)$.
(b) Find the equation of the plane which is perpendicular to the above line and passing through the point $(1,1,2)$.
B. Answer any 1 question from 32 to 33. Carries 4 scores.
32. Find the mean of the number obtained on a throw of an unbiased die.
33. Consider the planes $3 x-2 y+z+6=0$ and $2 x+y+2 z-6=0$ :
(a) Find the angle between the planes.
(b) Find the equation of the plane passing through the line of intersection of above planes and through the point $(0,0,0)$.

## PART - IV






















## PART - V

Answer any 2 questions from 34 to 36. Each carries 6 scores.
34. Solve the following system of equations by matrix method.

$$
\begin{array}{r}
x-y+2 z=1 \\
2 y-3 z=1 \\
3 x-2 y+4 z=2
\end{array}
$$

35. Find the following integrals :
(a) $\int \frac{x}{(x+1)(x+2)} \mathrm{d} x$
(b) $\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{4} x}{\sin ^{4} x+\cos ^{4} x} \mathrm{~d} x$
36. Solve the following linear programming problem graphically

$$
\text { Maximise } \quad Z=3 x+2 y
$$

Subject to

$$
\begin{array}{r}
x+2 y \leq 10 \\
3 x+y \leq 15 \\
x, y \geq 0
\end{array}
$$

## PART - V

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$$
(2 \times 6=12)
$$



$$
\begin{array}{r}
x-y+2 z=1 \\
2 y-3 z=1 \\
3 x-2 y+4 z=2
\end{array}
$$


(a) $\int \frac{x}{(x+1)(x+2)} \mathrm{d} x$
(b) $\int_{0}^{\frac{\pi}{2}} \frac{\sin ^{4} x}{\sin ^{4} x+\cos ^{4} x} \mathrm{~d} x$



Maximise $\quad Z=3 x+2 y$
Subject to

$$
\begin{array}{r}
x+2 y \leq 10 \\
3 x+y \leq 15 \\
x, y \geq 0
\end{array}
$$

